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**Management and economics of petroleum
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Fourth Class

Lecture (5)

By

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Depreciation Models

Depreciation – Definition

- **Depreciation** is the reduction of an asset's value over time.
- by:
 - Wear, Use, Deterioration, Obsolescence
- Why depreciation?
$$\text{Taxes} = (\text{income} - \text{expenses} - \text{depreciation}) (\text{tax rate})$$

Why depreciation?

- The capital investments of a corporation in tangible assets; equipment, computers, vehicles, buildings, and machinery are commonly recovered on the books of the corporation through depreciation.

Depreciable?

- Property is depreciable if it must:
 - be used in business
 - have a determinable useful life which is longer than one year
 - wear out, get used up, or become obsolete
 - not be inventory, stock in trade, or investment property
 - **Land is not depreciable** because it has an infinite life.

Problem

- Variable Cost per Unit = 1 SR
- Unit Price = 3 SR
- Machine First Cost = 50,000 SR
- Quantity Sold = 1 unit/year
- **Profit = ??????????????**

Solution

- Profit = Total Revenue – Total Cost
- Profit = $[1*3] - [1*1] = + 2 ?$
- Profit = $[1*3] - [(1*1) + 50,000] = - 49,998 ?$
- Profit = $[1*3] - [(1*1) + 8,000] = - 7,998 ?$

 **Depreciation**

Types of Depreciation

- **Book Depreciation**
 - Used for internal managerial decision making.
 - Management is free to use any method they so choose to compute book depreciation amounts
- **Tax Depreciation**
 - Used by a firm for income tax reporting
 - Follows strict rules and regulations.

Depreciation Methods

- Depreciation Methods
 1. Straight-Line Method (SL),
 2. Activity Method,
 3. Sum-of-the-Years Digits Method (SYD).

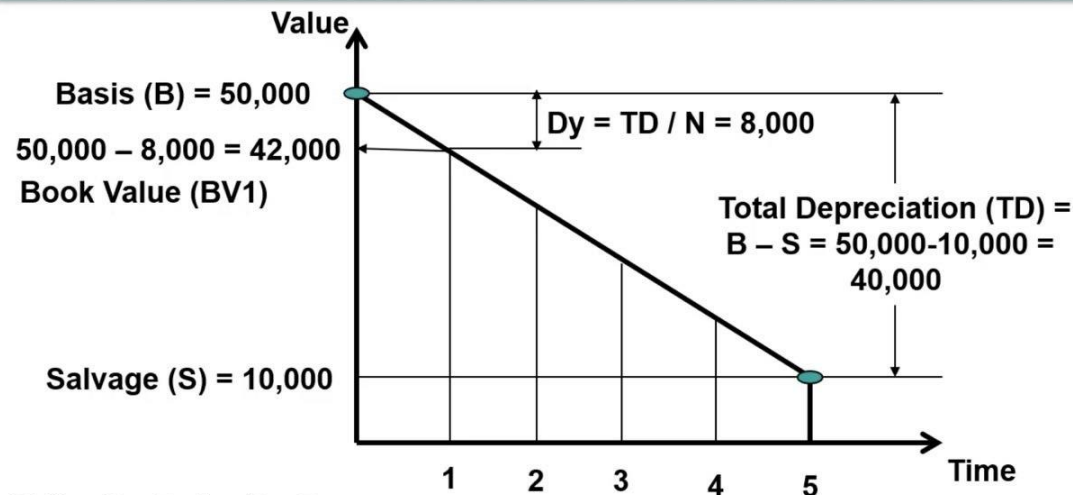
Straight-Line Method

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Example 1

- Given:
 - First cost or Basis (B) is \$50,000
 - Machine life (Recovery Period) is 5 years
 - Estimated salvage (S) of \$10,000.
- Required:
 - Depreciation rate (Dy)
 - The Book Value (BV) at the end of each year

Solution



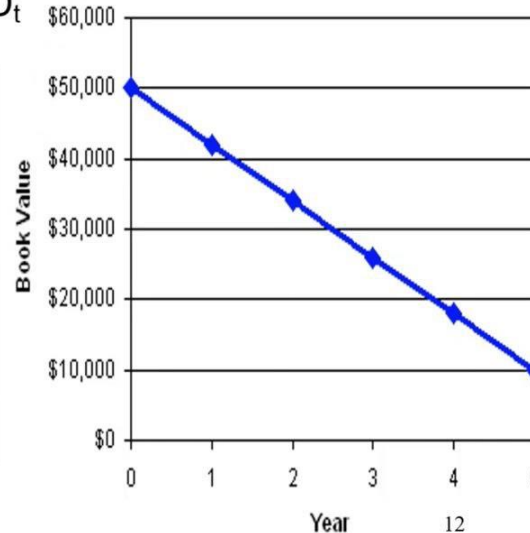
$$\begin{aligned} BV_1 &= B - Dy_1 = B - Dy \\ BV_2 &= BV_1 - Dy_2 \\ BV_3 &= BV_2 - Dy_3 \\ &\vdots \\ BV_N &= \text{Salvage value} \end{aligned}$$

Solution (Cont.)

SL depreciation: $D_t = (50,000 - 10,000) / 5 = \$8,000$

SL book value: $BV_t = BV_{t-1} - D_t$

Year, t	D_t	BV_t
0	0	\$50,000
1	8,000	42,000
2	8,000	34,000
3	8,000	26,000
4	8,000	18,000
5	8,000	10,000



Depreciation Terms

- **First Cost or Basis (B)** of an asset is:
 - Purchasing cost plus, Delivery costs plus, Installation costs and any other costs associated with preparing the asset for use.
- **Salvage Value (SV)** is the estimated market value at the end of the asset's useful life
 - Expressed as an estimated amount or as a percentage of the first cost

Salvage Value

- **Book Value** of an Asset (BV_t)
 - The remaining, undepreciated capital investment on the firm's books after the accumulated amounts of depreciation have been subtracted from the original cost basis.
- **Recovery Period** is Number of years over which basis of property is recovered through accounting process.

Straight-Line: The Standard (SL)

- Notations
 - B = The Basis or , first cost
 - N = The Recovery Period,
 - S = Estimated Salvage Value at $t = n$,
 - TD = The total depreciation = $B - S$
 - D_y = Annual depreciation charge = TD / N

Activity Method

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Activity Measures

Asset	Activity measure
Vehicles	Kilometers
Printer	Number of printed papers
Crane	Number of working hours

Example 2 (Activity Method)

Cost of crane	\$500,000
Estimated useful life	5 years
Estimated salvage value	\$ 50,000
Productive life in hours	30,000 hours

If the company used the crane for 4,000 hours in the first year, calculate:

1. The depreciation charge for the first year
2. The book value at the end of the first year

Solution

- $B = 500,000 \$$
- $S = 50,000 \$$
 - $TD = B - S = 500,000 - 50,000 = 450,000 \$$
- Life = 5 years or 30,000 hrs
 - $Dh = TD / Lh = 450,000 / 30,000 = 15 \$/\text{hr}$
- $Dy = Dh * \text{Working hours/year}$
 - $Dy1 = 15 * 4,000 = 60,000$
 - $BV1 = B - Dy1 = 500,000 - 60,000 = 440,000 \$$

Sum-of-the-Years' Digits Method

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Sum-of-the-Years'-Digits Method

- *Sum-of-the-Years'-Digits*. Each fraction uses the sum of the years as a denominator ($5 + 4 + 3 + 2 + 1 = 15$). The numerator is the number of years of estimated life remaining as of the beginning of the year.
- Alternate sum-of-the-years' calculation = $n(n+1) / 2$

Example 3 (SYD Method)

Cost of crane	\$500,000
Estimated useful life	5 years
Estimated salvage value	\$ 50,000
Productive life in hours	30,000 hours

Sum-of-the-Years'-Digits. Each fraction uses the sum of the years as a **denominator** ($5 + 4 + 3 + 2 + 1 = 15$). The **numerator** is the number of years of estimated life remaining as of the beginning of the year.

$$\text{Alternate sum-of-the-years' calculation} = n(n+1) / 2$$

SYD Method

Year	Dep. Fraction	Dep. Expenses	End of Year Book Value
1	5/15	$450,000 * (5/15) = 150,000$	$500,000 - 150,000 = 350,000$
2	4/15	$450,000 * (4/15) = 120,000$	$350,000 - 120,000 = 230,000$
3	3/15	$450,000 * (3/15) = 90,000$	$230,000 - 90,000 = 140,000$
4	2/15	$450,000 * (2/15) = 60,000$	$140,000 - 60,000 = 80,000$
5	1/15	$450,000 * (1/15) = 30,000$	$80,000 - 30,000 = 50,000$
Sum = 15	15/15=1	450,000	

Problem (1): The first cost of a machine is 15,000 SR with a life of 4 years or 1000 working hours and estimated salvage of 5,000 SR. if the company used this machine as shown in the following table:

year	1	2	3	4
Working hours	100	200	300	400

Calculate the book value at the end of the fourth year using:

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a) Straight line method

$$B = 15000 \text{ SR}$$

$$S = 5000 \text{ SR}$$

$$N = 4$$

$$TD = B - S = 15000 - 5000 = 10000 \text{ SR}$$

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$$Dy = \frac{TD}{N} = \frac{10000}{4} = 2500 \text{ SR/YEAR}$$

$$Bv_1 = B - Dy_1 = 15000 - 2500 = 12500 \text{ SR}$$

$$Bv_1 = B - Dy_1 = 15000 - 2500 = 12500 \text{ SR}$$

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$$Bv_2 = Bv_1 - Dy_2 = 12500 - 2500 = 10000 \text{ SR}$$

$$Bv_3 = Bv_2 - Dy_3 = 10000 - 2500 = 7500 \text{ SR}$$

$$Bv_4 = Bv_3 - Dy_4 = 7500 - 2500 = 5000 \text{ SR}$$

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b) Activity method

$$B = 15000 \text{ SR} \quad S = 5000 \text{ SR} \quad \text{life} = 1000 \text{ hours}$$

$$TD = B - S = 15000 - 5000 = 10000 \text{ SR}$$

$$Dh = \frac{TD}{\text{life}} = \frac{10000}{1000} = 10 \text{ SR/hr}$$

$$Dy = Dh * \text{working hours/year}$$

$$Dy = Dh * \text{working hours/year}$$

$$Dy_1 = 10 * 100 = 1000 \text{ SR}$$

$$Bv_1 = B - Dy_1 = 15000 - 1000 = 14000 \text{ SR}$$

$$Dy_2 = 10 * 200 = 2000 \text{ SR}$$

$$Bv_2 = Bv_1 - Dy_2 = 14000 - 2000 = 12000 \text{ SR}$$

$$Dy_3 = 10 * 300 = 3000 \text{ SR}$$

$$Dy_3 = 10 * 300 = 3000 \text{ SR}$$

$$Bv_3 = Bv_2 - Dy_3 = 12000 - 3000 = 9000 \text{ SR}$$

$$Dy_4 = 10 * 400 = 4000 \text{ SR}$$

$$Bv_4 = Bv_3 - Dy_4 = 9000 - 4000 = 5000 \text{ SR}$$

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c) sum-of-the-digits method

Year	Dep. Fraction	Dep. Exposures	End of year Book value
1	4/10	$10000 \times 4/10 = 4000$	$15000 - 4000 = 11000$
2	3/10	$10000 \times 3/10 = 3000$	$11000 - 3000 = 8000$
3	2/10	$10000 \times 2/10 = 2000$	$8000 - 2000 = 6000$
4	1/10	$10000 \times 1/10 = 1000$	$6000 - 1000 = 5000$
Sum = 10	10/10	1000	

problem (2): The first cost of a machine is 40,000 SR with a life of 5 years or 2,000 working hours and the estimated salvage of 10,000 SR. If the company used this machine as shown in the following table:

year	1	2	3	4	5
Working hours	500	300	400	300	500

Calculate the Book Value at the end of the five years using:

a) Activity method

$$B = 40000 \text{ SR} \quad S = 10000 \text{ SR} \quad \text{life} = 2000 \text{ Hours}$$

$$TD = B - S = 40000 - 10000 = 30000 \text{ SR}$$

$$Dh = \frac{TD}{\text{life}} = \frac{30000}{2000} = 15 \text{ SR/hr}$$

$$Dy = Dh * \text{working Hours/year}$$

$$Dy_1 = 15 * 500 = 7500 \text{ SR}$$

$$Bv_1 = B - Dy_1 = 40000 - 7500 = 32500 \text{ SR}$$

$$Dy_2 = 15 * 300 = 4500 \text{ SR}$$

$$Bv_2 = Bv_1 - Dy_2 = 32500 - 4500 = 28000 \text{ SR}$$

$$Dy_3 = 15 * 400 = 6000 \text{ SR}$$

$$Bv_3 = Bv_2 - Dy_3 = 28000 - 6000 = 22000 \text{ SR}$$

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$$Dy_4 = 15 * 300 = 4500 \text{ SR}$$

$$Bv_4 = Bv_3 - Dy_4 = 22000 - 4500 = 17500 \text{ SR}$$

$$Dy_5 = 15 * 500 = 7500 \text{ SR}$$

$$Bv_5 = Bv_4 - Dy_5 = 17500 - 7500 = 10000 \text{ SR}$$

$$Dy_5 = 15 * 500 = 7500 \text{ SR}$$

$$Bv_5 = Bv_4 - Dy_5 = 17500 - 7500 = 10000 \text{ SR}$$

b) Straight-Line Method

$$B = 40000 \text{ SR} \quad S = 10000 \text{ SR} \quad N = 5$$

$$TD = B - S = 40000 - 10000 = 30000 \text{ SR}$$

$$Dy = \frac{TD}{N} = \frac{30000}{5} = 6000 \text{ SR/year}$$

$$Bv_1 = B - Dy_1 = 40000 - 6000 = 34000 \text{ SR}$$

$$Bv_1 = B - Dy_1 = 40000 - 6000 = 34000 \text{ SR}$$

$$Bv_2 = Bv_1 - Dy_2 = 34000 - 6000 = 28000 \text{ SR}$$

$$Bv_3 = Bv_2 - Dy_3 = 28000 - 6000 = 22000 \text{ SR}$$

$$Bv_4 = Bv_3 - Dy_4 = 22000 - 6000 = 16000 \text{ SR}$$

$$Bv_5 = Bv_4 - Dy_5 = 16000 - 6000 = 10000 \text{ SR}$$

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3- Sum of digit method:

Year	Dep. Fraction	Dep. Exposures	End of year Book value
1	5/15	$30000 \times 5/15 = 10000$	$40000 - 10000 = 30000$
2	4/15	$30000 \times 4/15 = 8000$	$30000 - 8000 = 22000$
3	3/15	$30000 \times 3/15 = 6000$	$22000 - 6000 = 16000$
4	2/15	$30000 \times 2/15 = 4000$	$16000 - 4000 = 12000$
5	1/15	$30000 \times 1/15 = 2000$	$12000 - 2000 = 10000$
Sum = 15	15/15	30000	