

①

Chapter-4- (سائل سائل) liquid-liquid Extraction (Solvent Extraction)

The separation of the component of a liquid mixture by treatment with a solvent which one or more of the desired components is preferentially soluble is known as liquid-liquid Extraction. In the operation the liquid-mixture feed and the solvent are partially or completely immiscible.

Three stages are involved:

- 1- Bringing the feed mixture and the solvent into contact.
- 2- Separation of the two phase.
- 3- Removal and recovery of the solvent from each phase.

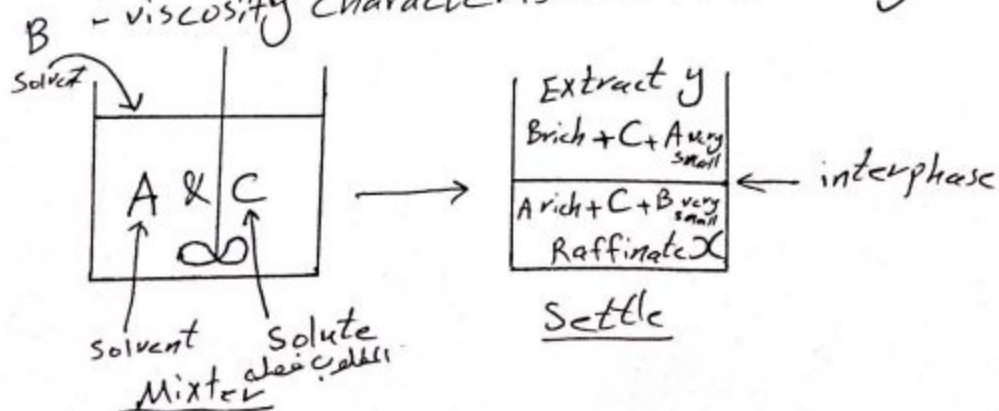
stage (1) and (2) is carried out in stage wise equipment (single piece of equipment) which is known as Mixer-Settler.

The operation of mixer-settler is:

- A- The mixing of the two liquid phase by agitation.
- B- The settling in a separate vessel by gravity.

* For example of liquid-liquid Extraction is the separation of aromatic from kerosene to improve their burning qualities.

And the separation of aromatic from paraffin and naphthenic compounds to improve the temperature - viscosity characteristic of lubricating oils.



By weight fraction:

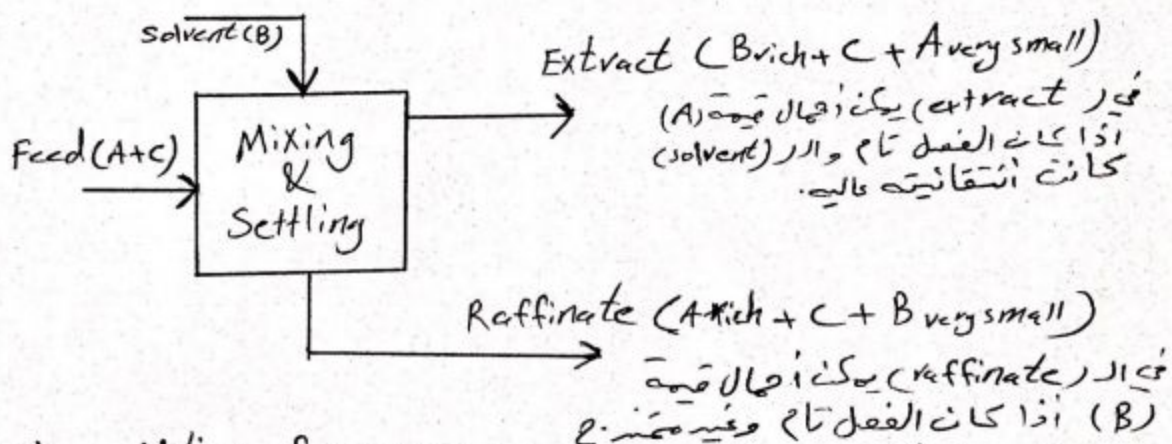
$$Y = \frac{C}{B+C+A^{\text{very small}}} = \left(\frac{C}{B+C}\right)_E$$

or $Y = \left(\frac{C}{B}\right)_E = \text{mass ratio of solute in extract}$

$$X = \frac{C}{A+C+B^{\text{very small}}} = \left(\frac{C}{A+C}\right)_R$$

$X = \left(\frac{C}{A}\right)_R = \text{mass ratio of solute in raffinate}$

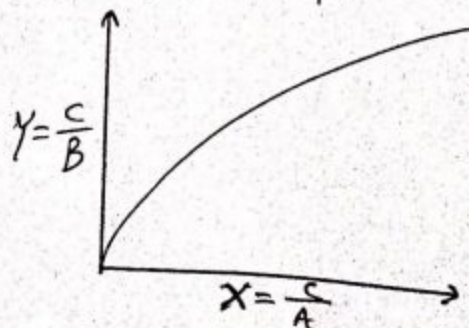
عندما مادتين متجانستين (miscible) موزعتين (A+C) نضيف مادة B (solvent) حيث تكون لها القابلية على حبس المادة C المذابة فيها من A (has good selectivity).



The addition of a new solvent to a binary mixture of (solute in a solvent) may lead to the formation of several types of mixture.

- 1- The solvent (B) may be completely immiscible with initial solvent (A). (فقد تام وغير متجانستين كلياً)

The equilibrium relation is shown by a plot of the concentration of solute in one phase against the concentration in the second phase.

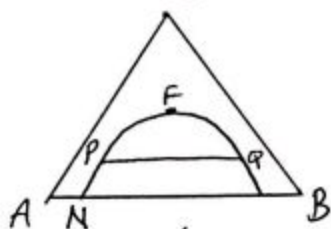


(3)

2- The homogenous solution may be formed, then the selected solvent (B) is unsuitable

تكوين سائل متجانس (فيه مفعول الى طبقتين) وفي هذه الحالة يكون
(مفضل جزئي) solvent المستعمل فيه ملائم.

3- The solvent (B) may be partially immiscible with the original solvent resulting in the formation of one pair of partially miscible liquid. Equilibrium are usually represented by triangular diagrams.



Choosing of solvent:

1- Good selectivity (β)

$$\beta = \frac{\text{wt. fraction of C in Extract} / \text{wt. fraction of A in Extract}}{\text{wt. fraction of C in Raffinate} / \text{wt. fraction of A in Raffinate}}$$

$$\beta = \frac{y_{CE} / y_{AE}}{x_{CR} / x_{AR}}$$

$$\beta > 1$$

the greater the value of β is the better in the extracting solvent.

2- good recoverability قابلية استعادة عالية

3- The liquid use may be have low viscosity.

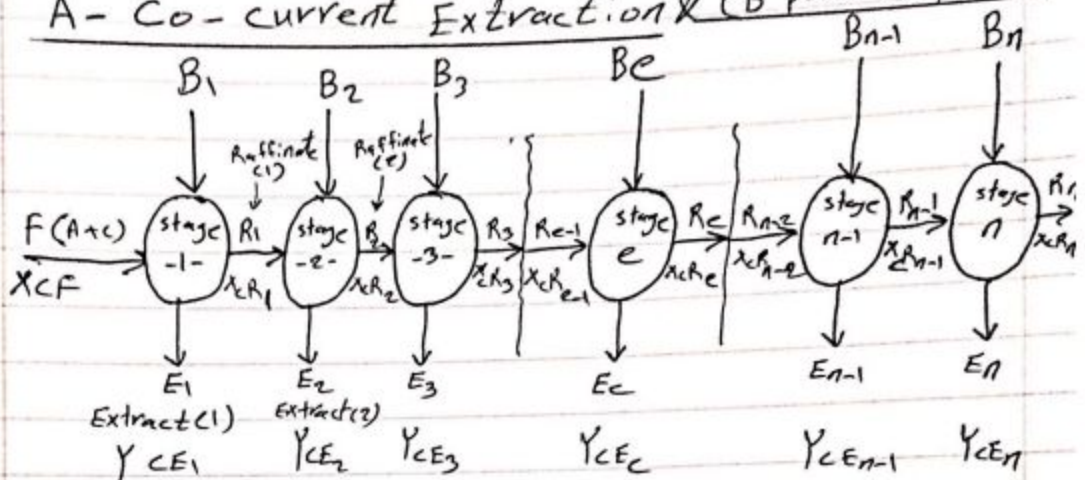
4- Density difference (the greater the density difference the quicker separator)

5- ويجب ان يكون خفيف سام ورفيع ولا يؤدي الى هرق العسل -
عند الاستعمال ولا يسبب التآكل ولا يتغير من درجة الحرارة والاهمية.

Extraction (2) أو ٢٥

(I) The solvent (B) may be completely immiscible with initial solvent (A). فقد المذيب الأولي

A - Co-current Extraction & (B pure component)



$$\text{wt. ratio } X = \frac{\text{wt. C}}{\text{wt. A}}$$

$$Y = \frac{\text{wt. C}}{\text{wt. B}}$$

component (C) mass balance on stage (1)

$$0 + A X_{CF} = A X_{R1} + B_1 Y_{CE1}$$

$$0 + A \times \frac{C}{A} = A \frac{C}{A} + B_1 \times \frac{C}{B_1}$$

$$\text{or } Y_{CE1} = \frac{-A}{B_1} (X_{R1} - X_{CF})$$

component (C) mass balance on stage (2)

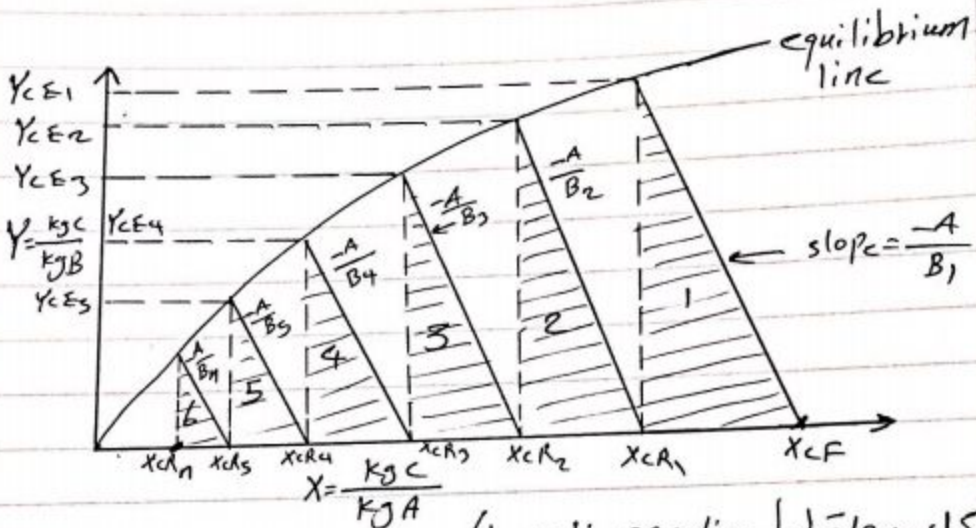
$$0 + A X_{R1} = A X_{R2} + B_2 Y_{CE2}$$

$$\text{or } Y_{CE2} = \frac{-A}{B_2} (X_{R2} - X_{R1})$$

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1)
$$Y_{CEn} = \frac{-A}{B_n} (X_{CRn} - X_{CRn-1})$$

operating line equation with slope = $\frac{-A}{B_n}$



(در هر مرحله عملیات با شیب متفاوتی انجام می‌دهیم) (در هر مرحله عملیات با شیب متفاوتی انجام می‌دهیم)
 $X_{CRn} \leftarrow X_{CF}$ در هر مرحله (در هر مرحله عملیات با شیب متفاوتی انجام می‌دهیم)

B- Co-current Extraction & B contain some amount of C having composition of Y_{CS}

Material Balance on stage (1)

$$A X_{CF} + B_1 Y_{CS} = A X_{CR1} + B_1 Y_{CE1}$$

$$Y_{CE1} = \frac{-A}{B_1} (X_{CR1} - X_{CF}) + Y_{CS}$$

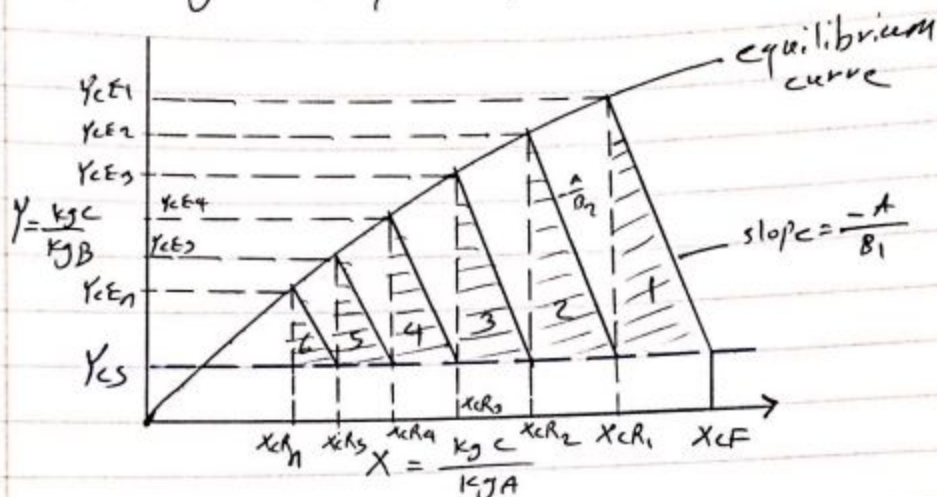
M.B on stage (n)

$$A X_{CRn-1} + B_n Y_{CS} = A X_{CRn} + B_n Y_{CEn}$$

$$Y_{CEn} = \frac{-A}{B_n} (X_{CRn} - X_{CRn-1}) + Y_{CS}$$

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operating line equation.



If B is added in a constant mass in each stage the slope of operating line will be constant, that means all the operating line will be parallel.

C - Co-current extraction and equilibrium data can be represented by a straight line
i.e. $Y = mX$ and the same amount of pure (B) is added in each stages.

component (C) Material Balance on stage (1)

$$A X_{CF} + 0 = A X_{CR1} + B Y_{CE1}$$

$$Y_{CE1} = m X_{CR1}$$

$$A X_{CF} = A X_{CR1} + B m X_{CR1}$$

$$X_{CR1} = \left(\frac{A}{A + Bm} \right) X_{CF} \quad \text{--- (1)}$$

component (C) Material Balance on stage (2)

$$A X_{CR1} + 0 = A X_{CR2} + B Y_{CE2}$$

$$A X_{CR1} = A X_{CR2} + B m X_{CR2}$$

⑦

$$X_{CR2} = \left(\frac{A}{A+Bm} \right) X_{CR1} \text{ --- (2)}$$

$$X_{CR2} = \left(\frac{A}{A+Bm} \right)^2 X_{CF} \text{ --- (3)}$$

$$X_{CRn} = \left(\frac{A}{A+Bm} \right)^n X_{CF} \text{ --- (4)}$$

The number of stage required to go from X_{CF} to $X_{CRn} = n$

$$\frac{X_{CRn}}{X_{CF}} = \left(\frac{A}{A+Bm} \right)^n$$

$$\ln \frac{X_{CRn}}{X_{CF}} = n \ln \left(\frac{A}{A+Bm} \right)$$

$$n = \frac{\ln \frac{X_{CRn}}{X_{CF}}}{\ln \frac{A}{A+Bm}}$$

n = Number of stage required.

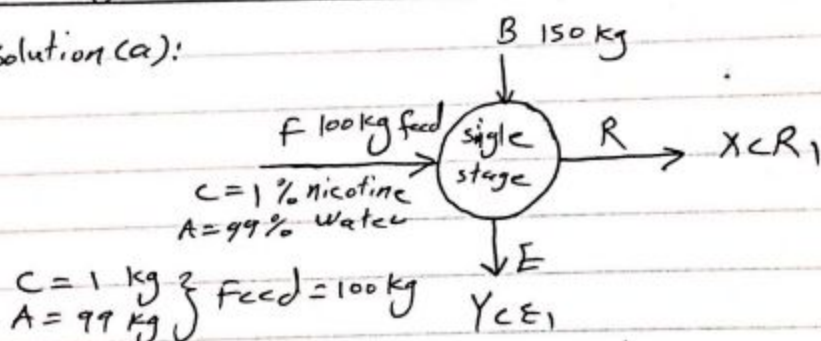
(3)

Example: Nicotine (C) in a water (A) solution containing 1% nicotine is to be extracted with kerosen (B) at 20°C . Water & kerosen are essentially insoluble. a) Determine the percentage extraction of nicotine if 100 kg of feed solution is extracted once with 150 kg solvent (one stage). (b) Repeat for three continuous theoretical stage extractions using 50 kg solvent in each stage.

Equilibrium data are:

X	$\frac{\text{kg nicotine}}{\text{kg water}}$	0	0.001	0.0024	0.005	0.0075	0.0099	0.02
Y	$\frac{\text{kg nicotine}}{\text{kg kerosine}}$	0	0.0008	0.0019	0.0045	0.0068	0.0091	0.018

Solution (a):



$$\left. \begin{array}{l} C = 1 \text{ kg} \\ A = 99 \text{ kg} \end{array} \right\} \text{Feed} = 100 \text{ kg}$$

$$X_{CF} = \frac{C}{A} \text{ in feed} = \frac{1}{99} = 0.0101$$

$$\frac{-A}{B} = \frac{-99}{150} = -0.66 \text{ slope of operating line}$$

From X_{CF} in drawing of X & Y draw line FD with a slope of -0.66 and Find:

$$X_{CR1} = 0.00425 \frac{\text{kg nicotine}}{\text{kg water}} = \frac{C}{A}$$

$$Y_{CE1} = 0.0038 \frac{\text{kg nicotine}}{\text{kg kerosine}} = \frac{C}{B}$$

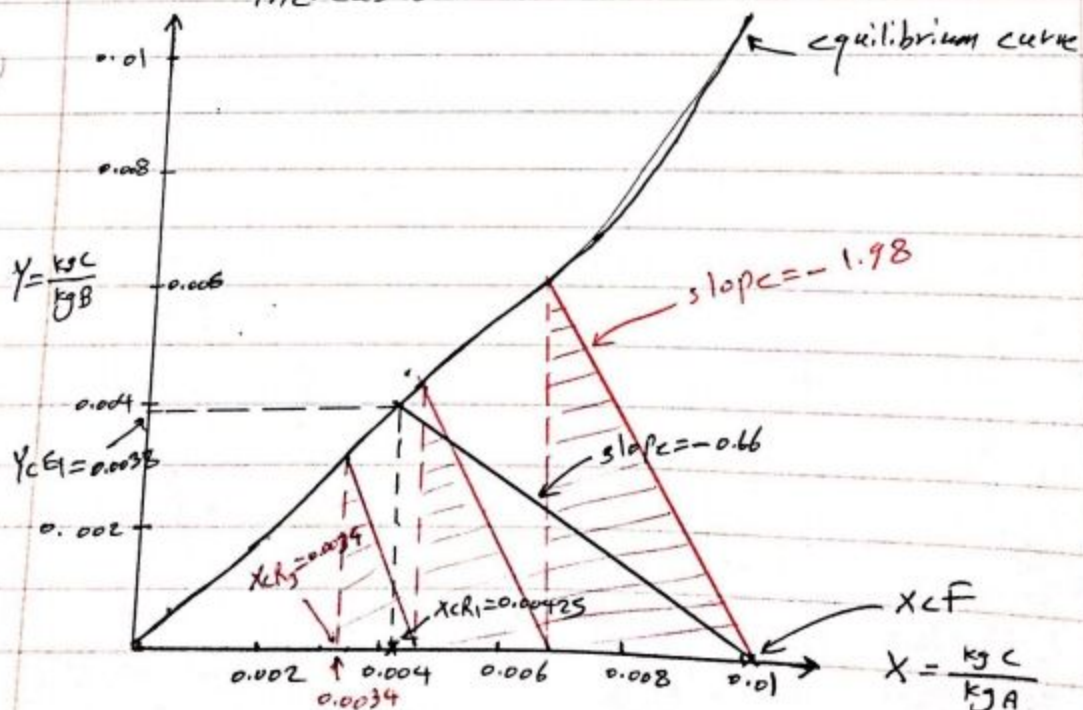
⑦

The nicotine removed from water = $\left(0.0101 \frac{\text{kg nicotine}}{\text{kg water}} - \frac{0.004 \text{ kg nicotine}}{\text{kg water}}\right) \times 99 \text{ kg water}$
 $= 0.58 \text{ kg}$
 $= 58\% \text{ percent extraction of nicotine}$

b) For each stage, the slope of operating line
 $= -\frac{A}{B} = \frac{50}{99} = -1.98$
 from x_{CF} in the drawing, draw three stage with slope $= -1.98$. we find that the final raffinate composition is $x_{R3} = 0.0034$

$\therefore$ The nicotine removed from water
 $= \left(0.0101 \frac{\text{kg nicotine}}{\text{kg water}} - 0.0034 \frac{\text{kg nicotine}}{\text{kg water}}\right) \times 99 \text{ kg water}$
 $= 0.663 \text{ kg}$
 $= 66.3\% \text{ of that in the feed}$

Notice: when we use three stages the % removed increased.



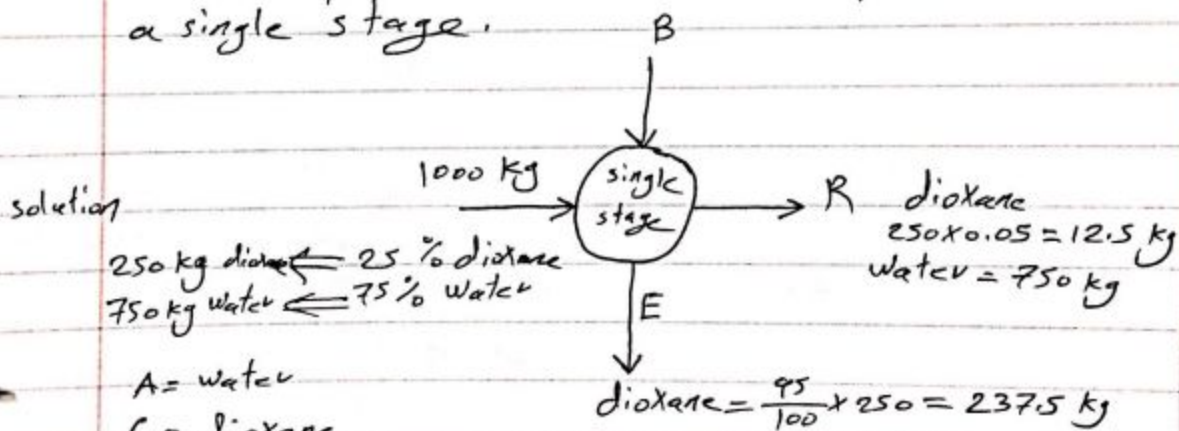
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Example: Water dioxane solution for a minimum boiling Azeotrope at atm. pressure and can not be separated by ordinary distillation method. Benzene forms no Azeotrope with dioxane and may be used as an Extracting solvent etc. The equilibrium distribution of dioxane between water & benzene is as follows.

wt.% dioxane in water (X) 0.051 0.189 0.252

wt.% dioxane in Benzene (Y) 0.052 0.225 0.32

The feed is 1000 kg of 25% dioxane & 75% water and Extraction design to remove 95% of dioxane. Find the quantity of solvent (B) required in a single stage.



A = water

C = dioxane

B = Benzene

$$y = \frac{C}{C+B} = \frac{\frac{C}{B}}{\frac{C}{B} + \frac{B}{B}} = \frac{Y}{Y+1}$$

$$\therefore Y = \frac{y}{1-y}$$

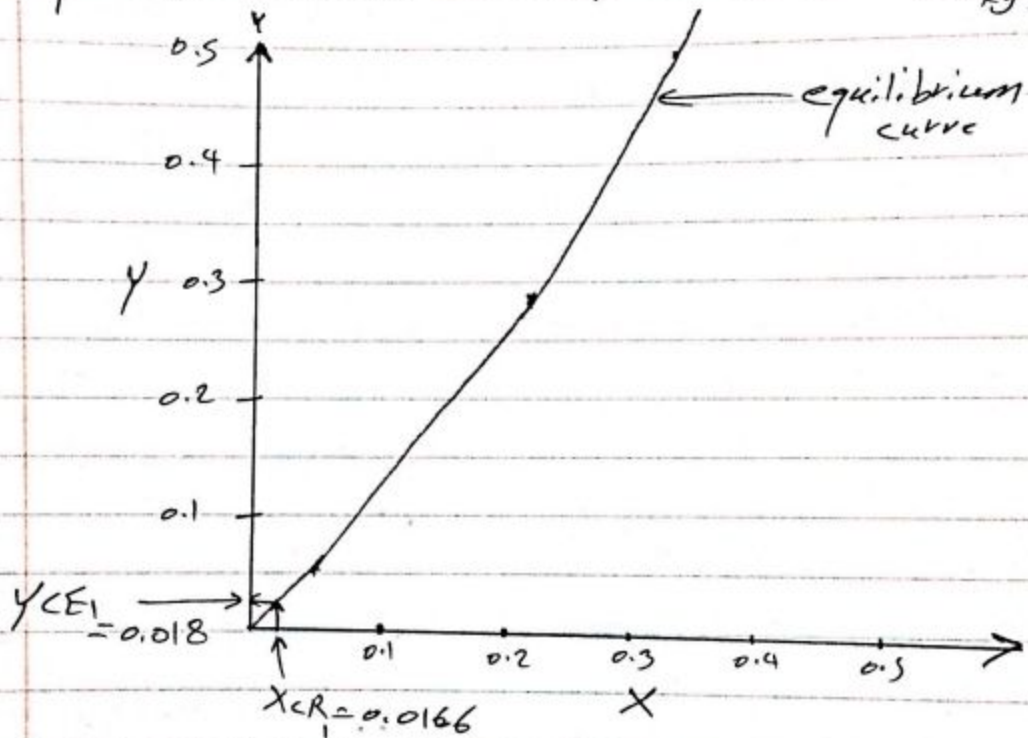
$$x = \frac{C}{C+A} = \frac{\frac{C}{A}}{\frac{C}{A} + \frac{A}{A}} = \frac{X}{X+1}$$

$$X = \frac{x}{1-x}$$

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$$X_{CR} = \frac{C}{A} = \frac{12.5 \text{ kg dioxane}}{750 \text{ kg water}} = 0.0166$$

Mass Ratio	ال	Mass fraction in equilibrium	يمثل	
X	0	0.0537	0.233	0.337 $\frac{\text{kg dioxane}}{\text{kg water}}$
Y	0	0.055	0.29	0.47 $\frac{\text{kg dioxane}}{\text{kg benzene}}$



From Diagram above

$$X_{CR} = 0.0166 \Rightarrow Y_{CE1} = 0.018 \frac{\text{kg dioxane}}{\text{kg benzene}}$$

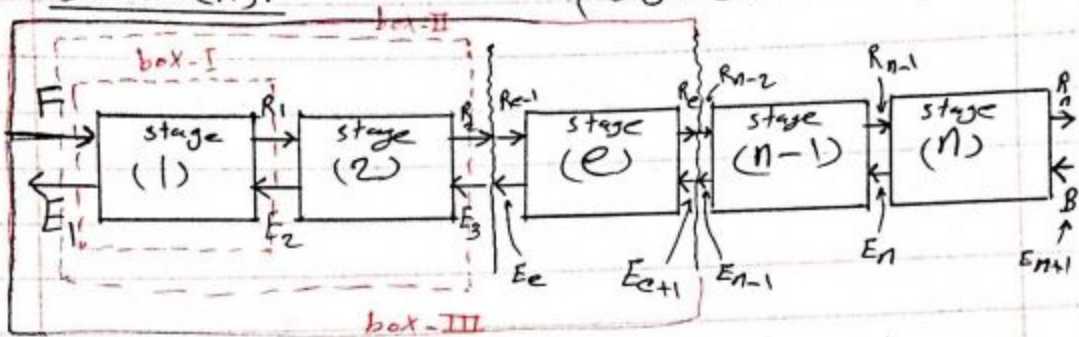
$$0.018 = \frac{237.5 \text{ kg dioxane}}{B}$$

$$\therefore B = \frac{237.5}{0.018} = 13194 \text{ kg}$$

(12)

D- counter current extraction :

Solvent (B) may be completely immiscible with initial solvent (A).
 المذيب (B) قد يكون متفصل تام



All Raffinate stream (R) contain $\frac{C}{A}$ only
 All Extract stream (E) contain $\frac{C}{B}$ only
 component C material balance on 1st stage box-I
 $AX_cF + BY_cE_2 = AX_cR_1 + BY_cE_1$

$$Y_cE_2 = \frac{A}{B} (X_cR_1 - X_cF) + Y_cE_1$$

Material Balance on 2nd stage box-II

$$AX_cF + BY_cE_3 = AX_cR_2 + BY_cE_1$$

$$Y_cE_3 = \frac{A}{B} (X_cR_2 - X_cF) + Y_cE_1$$

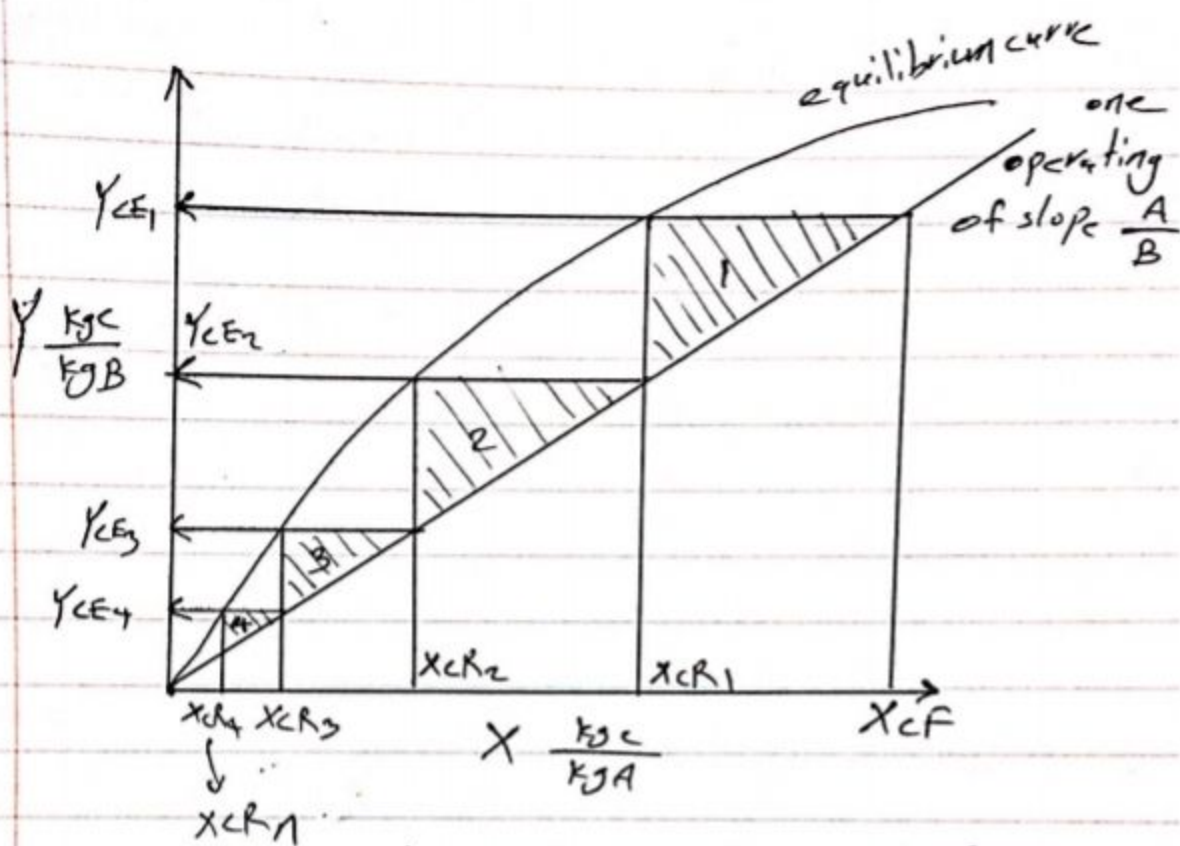
Material Balance on eth stage box-III

$$AX_cF + BY_cE_{e+1} = AX_cR_e + BY_cE_1$$

$$Y_cE_{e+1} = \frac{A}{B} (X_cR_e - X_cF) + Y_cE_1$$

operating line of slope $\frac{A}{B}$ وهناك خط تشغيل واحد
 في الاتجاه العكسي

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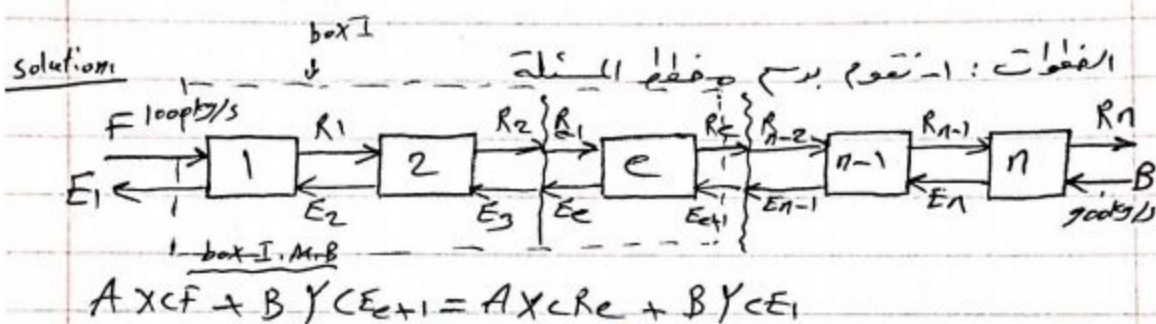


4 stages to go from $X_{CF} \rightarrow X_{CR1}$

Example: 1000 kg/s of feed contain 25% C & 75% A with 900 kg/s of solvent B in a counter current extraction system with totally immiscible between two solvent. How many theoretical stage required to remove 95% of the solute C?

The equilibrium data are:

X kgC/kgA	0	0.0537	0.233	0.33
Y kgC/kgB	0	0.055	0.29	0.37



$$Y_{CE_{n+1}} = \frac{A}{B} (X_{CR_n} - X_{CF}) + Y_{CE_1} \quad \rightarrow \text{operating line equation}$$

تقوم بإيجاد معادلة operating line وذلك بإيجاد X_{CR_n} و Y_{CE_1} و X_{CF} و $\frac{A}{B}$ و Y_{CE_1} و X_{CF}

$$\begin{aligned} C \text{ in feed} &= 250 \text{ kg/s} \\ A \text{ in feed} &= 750 \text{ kg/s} \end{aligned} \quad \left\{ \begin{aligned} X_{CF} &= \frac{\text{kgC}}{\text{kgA}} = \frac{250}{750} = 0.333 \end{aligned} \right.$$

$$B = 900 \text{ kg/s} \Rightarrow \frac{A}{B} = \frac{750}{900} = 0.833$$

$$\text{amount of recovered C in extract} = 250 \times 0.95 = 237.5 \text{ kg/s}$$

$$\text{amount of C in final raffinate} = 250 \times 0.05 = 12.5 \text{ kg/s}$$

$$Y_{CE_1} = \frac{\text{kgC}}{\text{kgB}} = \frac{237.5}{900} = 0.263$$

$$X_{CR_n} = \frac{\text{kgC}}{\text{kgA}} = \frac{12.5}{750} = 0.0167$$

$$Y_{CE_{n+1}} = 0.833 (X_{CR_n} - 0.333) + 0.263$$

$$Y_{CE_{n+1}} = 0.833 X_{CR_n} - 0.0149$$

operating line + equilibrium curve

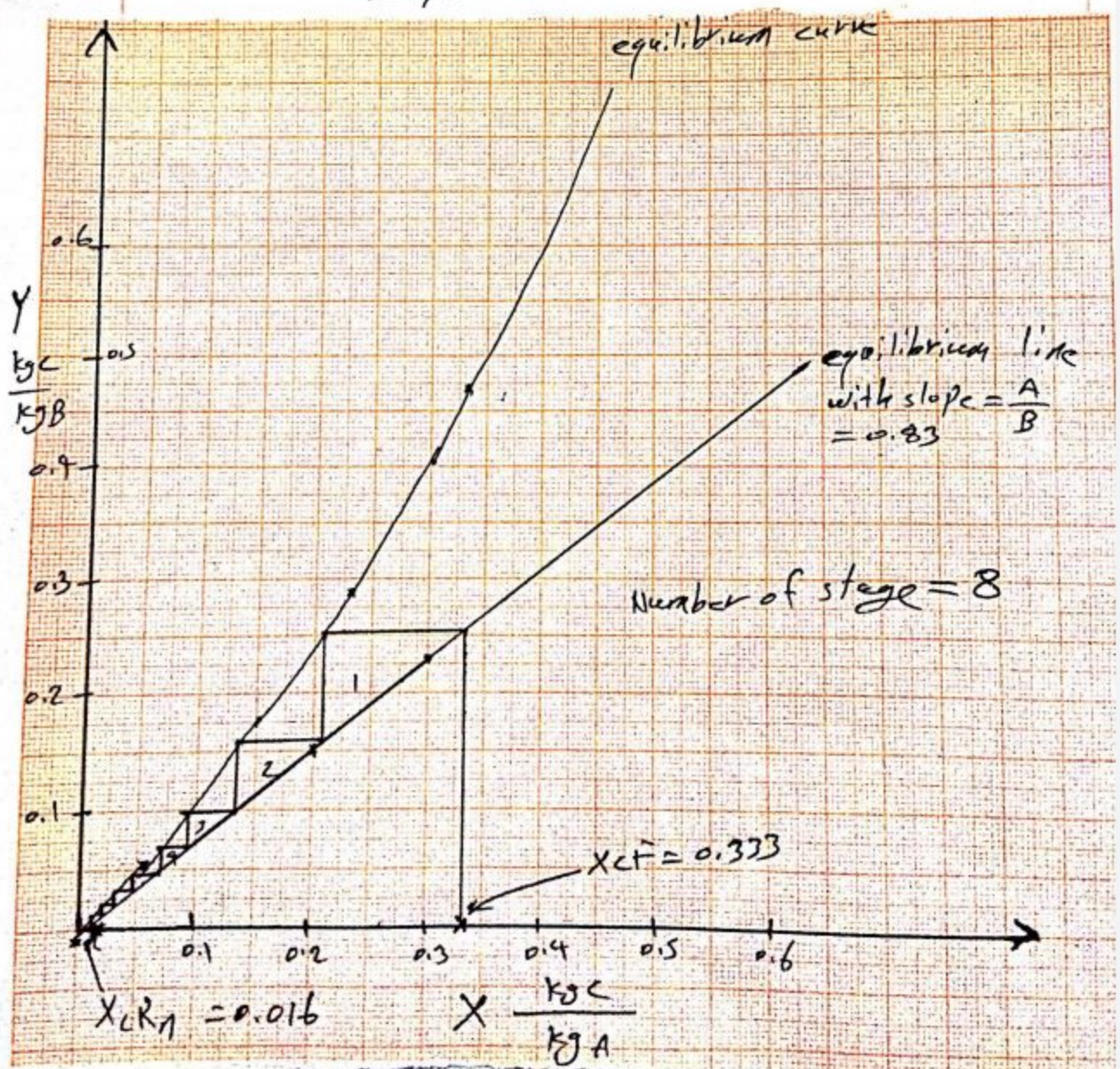
و منبج عدد المراحل من X_{CF} إلى X_{CR1}
 $X_{CR1} = 0.0161$ $X_{CF} = 0.333$

$$Y_{CE_{n+1}} = 0.833 X_{CRc} - 0.0144$$

$$X=0 \Rightarrow Y = -0.0144$$

$$X=0.2 \Rightarrow Y = 0.1522$$

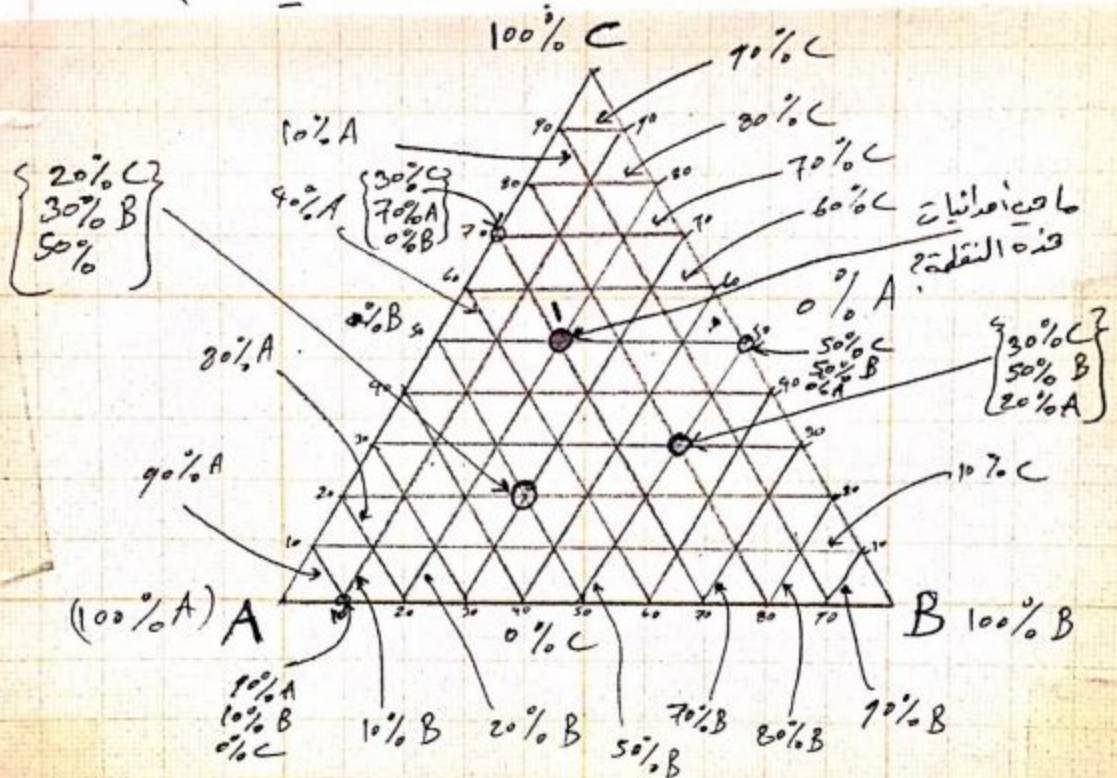
$$X=0.3 \Rightarrow Y = 0.235$$



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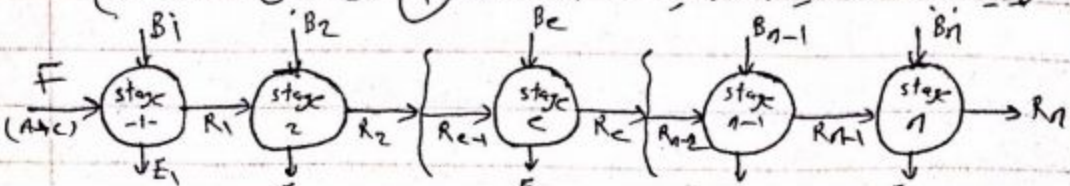
II) The solvent (B) may be partially miscible with the original solvent (فصل في نظام (فصل جزئي)

Equilibrium are usually represented by triangular diagrams. أي تكون حالة التوازن ممثلة بالمثلث كما في الرسم أدناه

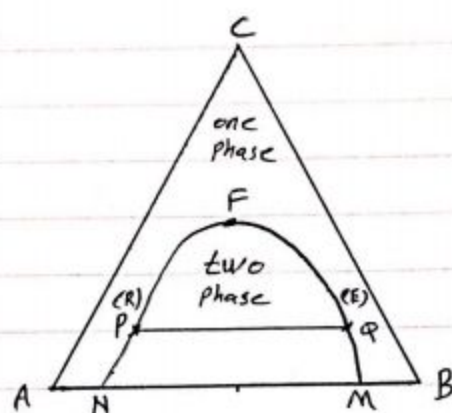


يتم تقسيم المثلث المساري الأضلاع بالساري إلى 10 أجزاء حيث أي نقطة داخل المثلث تكون أمثلياً لها
ممكنة من A, B, C أما في أي ضلع من أضلاع المثلث
تكون الأمثليات من مادتين فقط لأن المادة الثالثة
نسبتها صفر.

يتم متابعة نقاط المثلث بأصابع
ويجب تحديد الأمثليات النقطة 1 من قبل الطلبة



(17)



This is the most common type of system in extraction and typical examples are water (A) - chloroform (B) - acetone (C).

- * The solute C is completely miscible with two solvents A & B but two solvents A & B are partially miscible with each other.
- * Liquid C dissolves completely in A & B but A & B dissolve only to a limited extent in each other to give saturated liquid solutions at N (A-rich) and M (B-rich).
- * The distance AN represents the solubility of solvent B in A, and MB represents the solubility of solvent A in B.
- * Curve NPFQM is the binodal solubility curve. Any mixture outside this curve will be a homogeneous solution of one liquid phase. The area under the curve represents a two-phase region which splits up into two layers in equilibrium with each other.

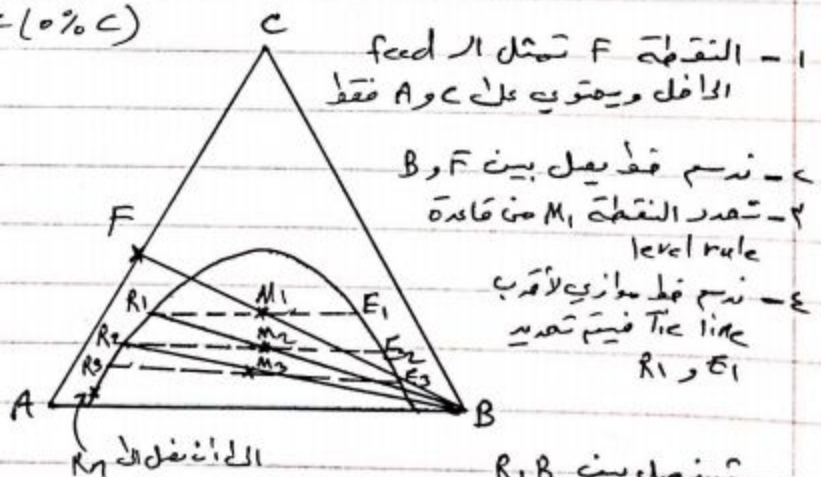
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- * These layers have composition represented by point p and Q and pQ is known as tie line.
- * point F represent a single phase which does not split into two phase which is known as a plait point.
- * point F is fixed if either the temperature and pressure is fixed, F نقطة ثابتة مع الضغط أو الحرارة أو التركيز أو تنزل إلى الأسفل بتغيير درجة الحرارة أو التركيز
- * The side of CB known as Extract (E) $\rightarrow Q$
The side of CA known as Raffinate (R) $\rightarrow p$

(A) Co-current extraction and solvent A and B are partially miscible مخلوط جزئی

The solution is done graphically

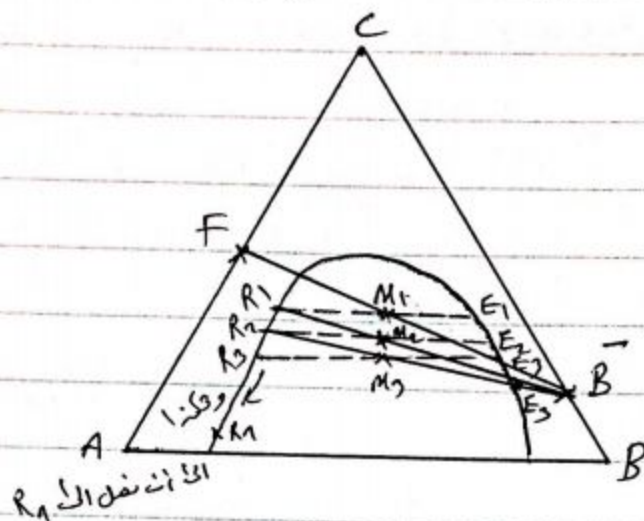
- 1- The solvent B is pure (0% C)



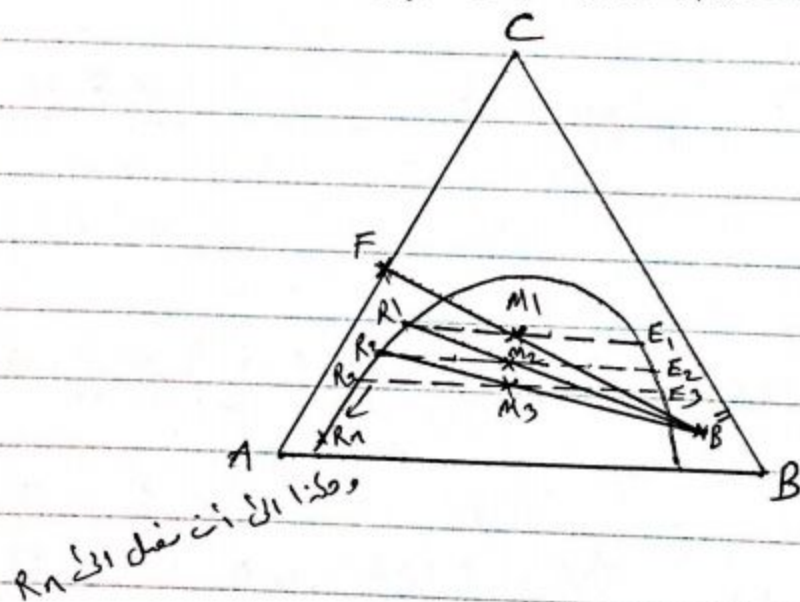
- ٥- تم فصل بين R_1 و R_2 إلى أن فصل إلى R_1
٦- مصدر M_2 من قاعدة l_{catalak}
٧- ندرس فقط موازٍ لأقطاب T_k line فيتم تسعير R_2 R_1
نذكر الخطوات إلى أن فصل إلى R_1 والذي يحوي على أمثلة
منه من C .

(19)

2- The solvent ($\bar{B}$) contains some of c



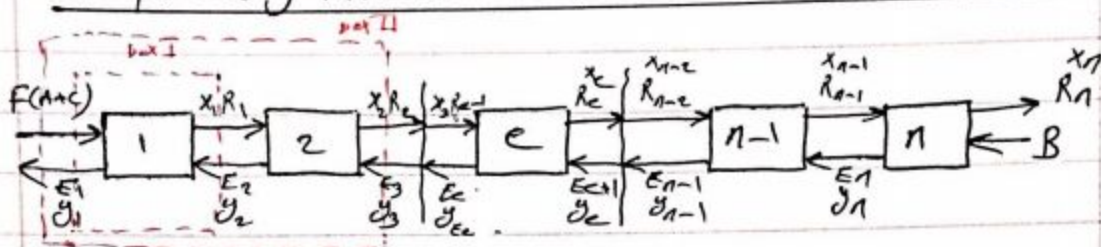
3- The solvent ($\bar{B}$) contains A & C



ملاحظة:
بالنسبة لهذا النوع فقط الرسوم مقلوبة
ولا توجد أمثلة.

(20)

(B) - Counter current extraction and solvent (B) is partially miscible with solvent A



Material balance on 1st stage (box I)

$$F + E_2 = R_1 + E_1$$

$$F - E_1 = R_1 - E_2 = P \text{ constant}$$

Material balance on stage (2) (box II)

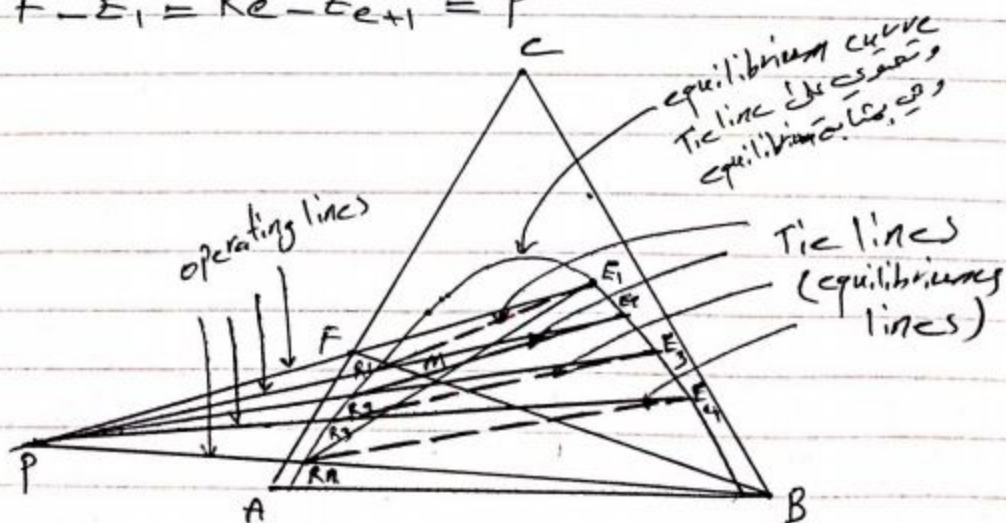
$$F + E_3 = R_2 + E_1$$

$$F - E_1 = R_2 - E_3 = P$$

Material balance on eth stage

$$F + E_{e+1} = R_e + E_1$$

$$F - E_1 = R_e - E_{e+1} = P$$



خطوات العمل :

- ١- نحدد نقطة F على خط AC في المثلث بواسطة معرفة نسبة C و A
- ٢- نحدد نقطة M وذلك بإكمال المستقيم FB ومن نسبة F و B ومقابلة level Rule .
- ٣- تحديد R_1 وذلك من خلال معرفتنا بنسبة الفصل في (final % C extractor)
- ٤- نقل $R_1 M$ فيقطع خط الـ equilibrium curve في E_1
- ٥- نحدد E_1 مع اقتراب Tie line أو موازي له فنحدد R_1
- ٦- نجد E_2 بعد PR_1 الى ان يقطع equilibrium curve
- ٧- نجد R_2 بعد E_2 موازي الى اقتراب Tie line فيقطع equilibrium curve في R_2
- ٨- اكمال PR_2 فيقطع Equilibrium curve في E_3
- ٩- اكمال R_3 بواسطة Tie line أو اقتراب Tie line موازي وهكذا الى ان نقل الى R_1 ونشاهد نسبة المراحل

ملاحظة مهمة :

لتحديد نقطة P وذلك بعد $E_1 F$ و $R_1 B$ فيتمثلان من نقطة P وايضاً تكون يميناً أو يساراً .

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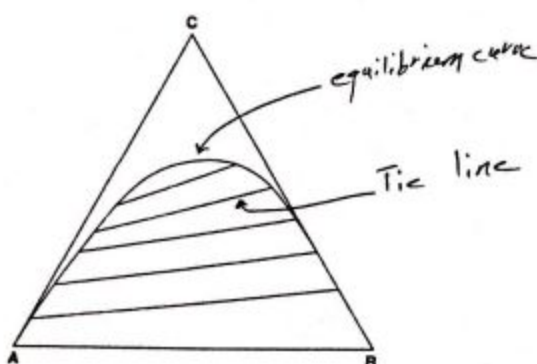


Figure 13.17. Equilibrium data for Example 13.2.

Solution

The equilibrium data are replotted in Figure 13.18 and F, representing the feed, is drawn in on AC at $C = 0.50$, $A = 0.50$. FB is joined and M located such that $FM/MB = 0.25$. R_2 is located on the equilibrium curve such that $C = 0.15$. In fact $B = 0.01$ and $A = 0.84$. E_1 is located by projecting R_2M on to the curve and the pole P by projecting E_1F and BR_2 . R_1 is found by projecting from

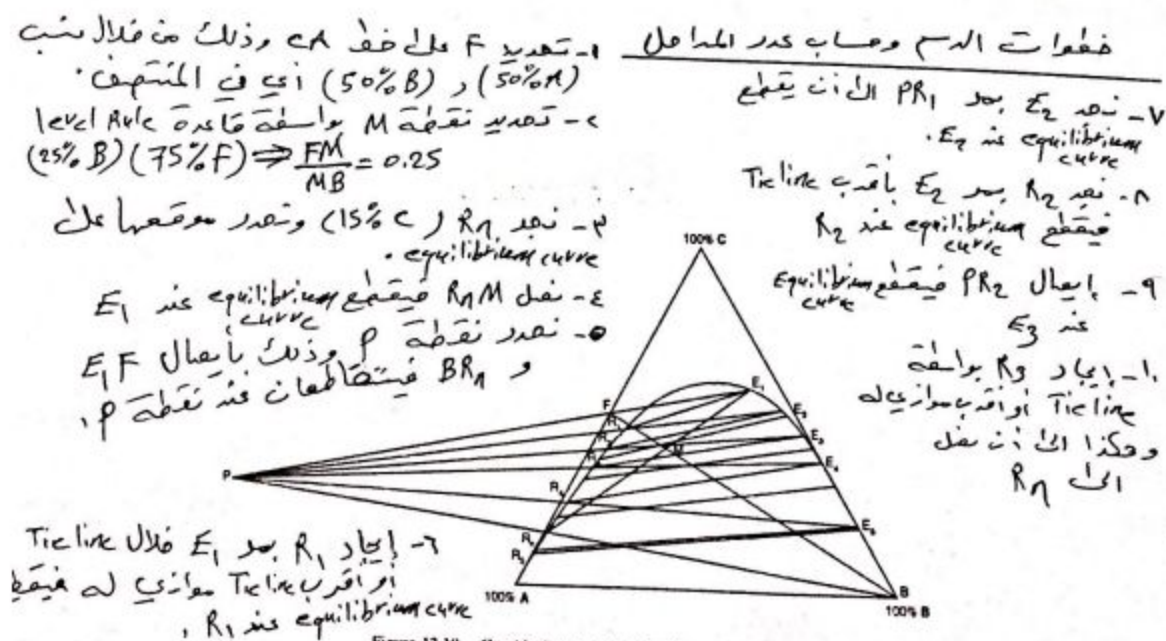


Figure 13.18. Graphical construction for Example 13.2

E_1 along a tie-line and E_2 as the projection of PR_1 . The working is continued in this way and it is found that R_5 is below R_* and hence 5 ideal stages are required.

From Figure 13.18 the concentration of extract E_1 is 9 per cent A, 58 per cent C, and 33 per cent B.

example

2

It is proposed to reduce the concentration of acetaldehyde in aqueous solution from 50 per cent to 5 per cent by mass, by extraction with solvent S at 293 K. If a countercurrent multiple-contact process is adopted and 0.025 kg/s of the solution is treated with an equal quantity of solvent, determine the number of theoretical stages required and the mass flowrate and concentration of the extract from the first stage.

23

The equilibrium relationship for this system at 293 K is:

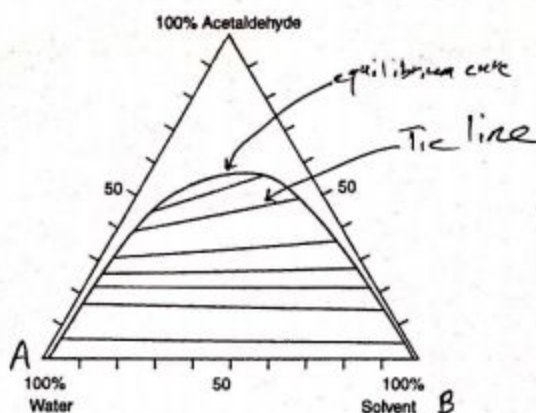


Figure 13a. Equilibrium data for Problem 13.9

Solution

The data are replotted in Figure 13b and the point F, representing the feed, is drawn in at 50 per cent acetaldehyde, 50 per cent water. Similarly, R_n , the raffinate from stage n located on the curve corresponding to 5 per cent acetaldehyde. (This solution then contains 2 per cent S and 93 per cent water.) FB is joined and point M located such that $FM = M$, since the ratio of feed solution to solvent is unity. R_nM is projected to meet the equilibrium curve at E_1 and FE_1 and R_nB are projected to meet at P. The tie-line E_1R_1 is drawn in and the line R_1P then meets the curve at E_2 . The working is continued in this way and it is found that R_4 is below R_n and hence four theoretical stages are required.

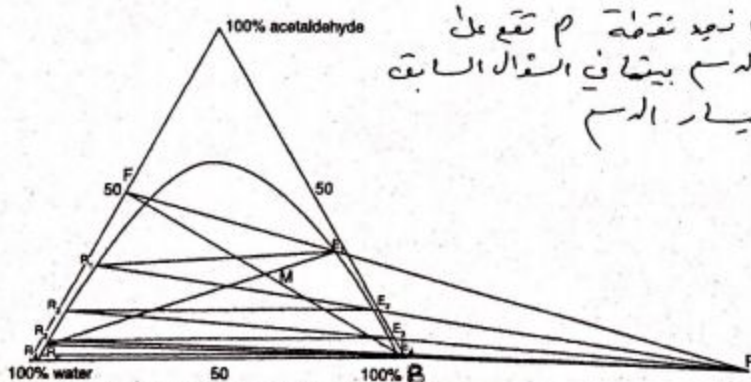


Figure 13b. Graphical construction for Problem 13.9

From Figure 13b, the composition of the extract from stage 1, E_1 , is:

3 per cent water, 32 per cent acetaldehyde, and 65 per cent

Making an overall balance, $F + S = R_n + E_1$

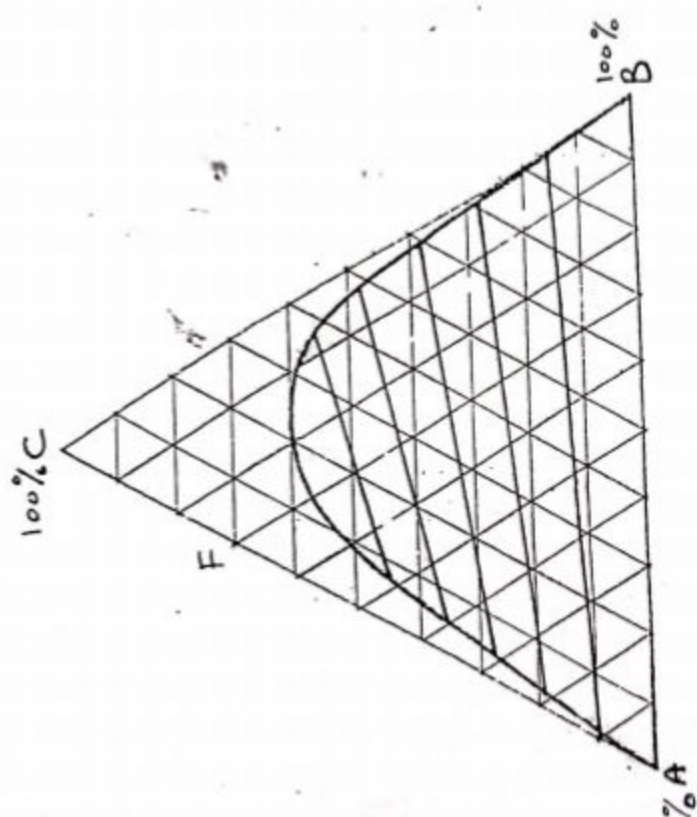
Thus: $(0.025 + 0.025) = (R_n + E_1) = 0.050 \text{ kg/s}$

Making an acetaldehyde balance:

$$(0.50F + 0) = (0.05R_n + 0.32E_1)$$

$$0.05(0.050 - E_1) + 0.32E_1 = (0.50 \times 0.025) \quad \text{and} \quad \underline{E_1 = 0.037 \text{ kg/s}}$$

أرجو من الطلبة حل المثال التالي على هذه الورقة



(2.4)

أرجو من طيبة على المثال الأول على هذه الورقة -

